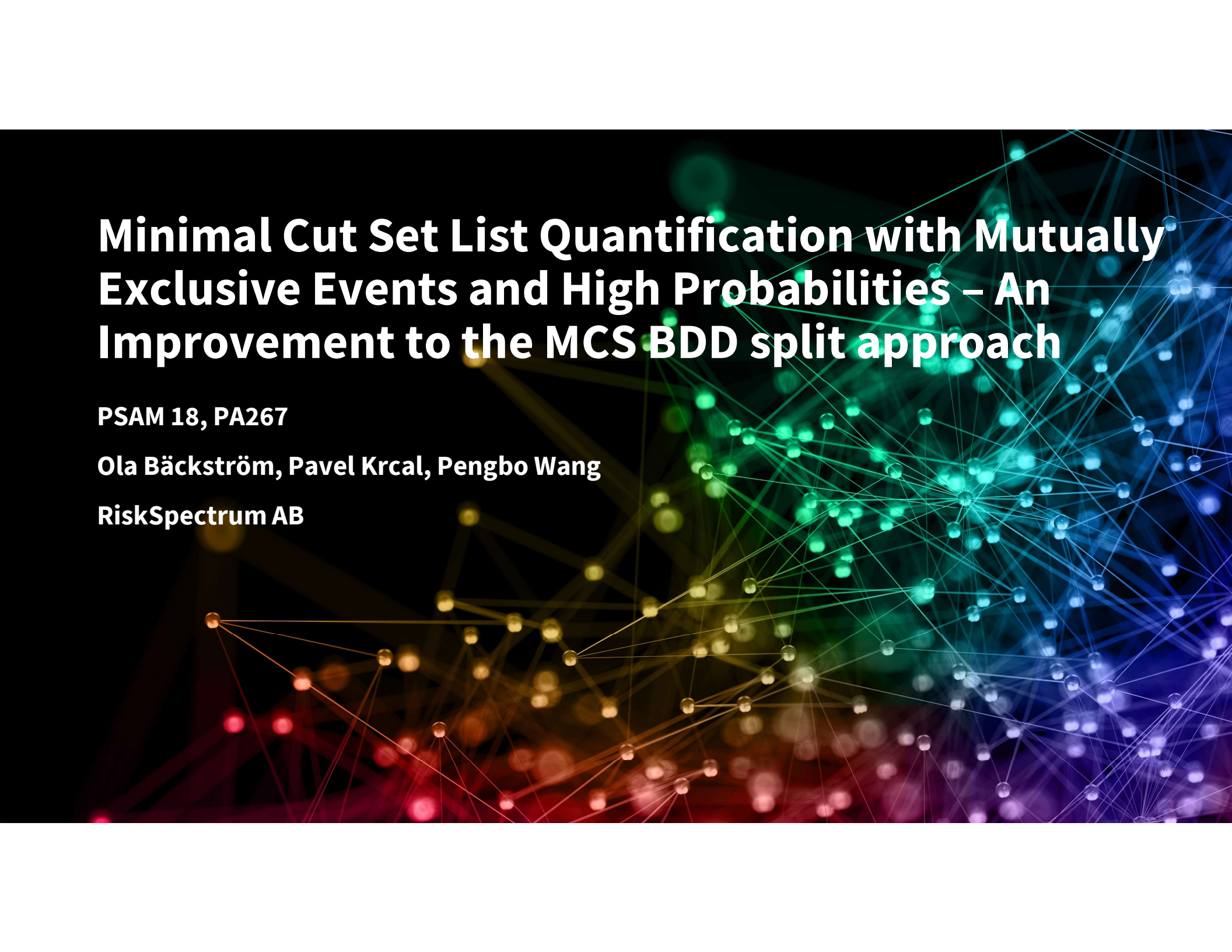




Minimal Cut Set List Quantification with Mutually Exclusive Events and High Probabilities – An Improvement to the MCS BDD split approach

PSAM 18, PA267

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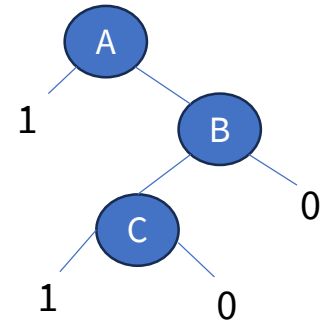
RiskSpectrum AB

Introduction

- Presentation about a recent development of the MCS BDD approach in RiskSpectrum
- Focusing on a potential accuracy issue in corner case scenarios, mostly in seismic risk assessments
- Introduce the approach to increase (solve) the accuracy in these scenarios

BDD approach and overview of RiskSpectrum MCS BDD

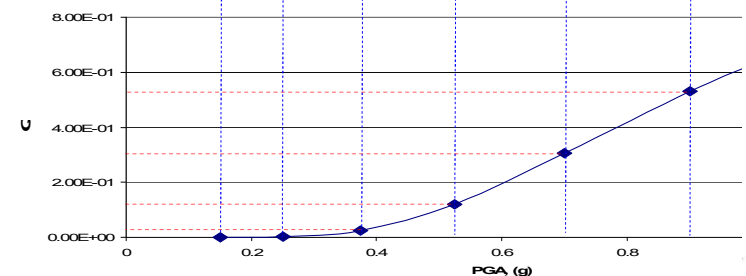
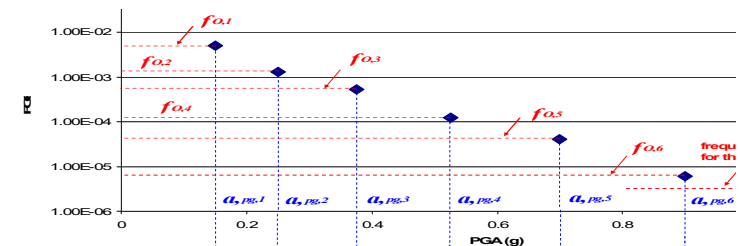
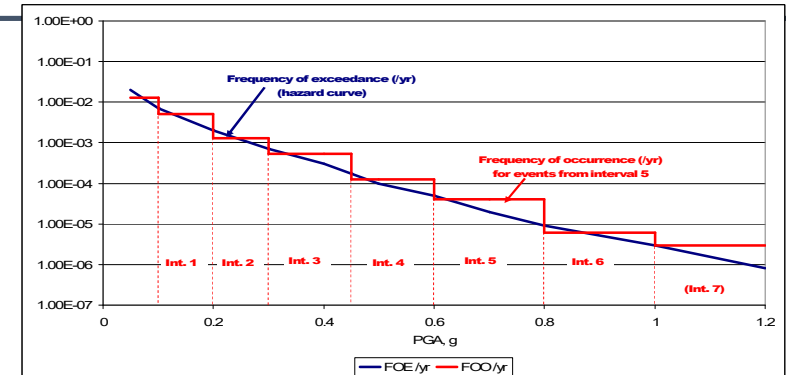
- Pivotal decomposition method
- Both failure and success branches are being developed
- When all branches have reached state “1” or “0” the problem is solved
- Example, MCS list: {A, BC}
- Why MCS BDD: Very good accuracy in calculations – also considering success and high probabilities
- RiskSpectrum approach - scalability:
 - Split of the MCS list into a part treated by BDD and a part treated by MCUB
 - Use of exact and approximate BDD nodes
 - Control of number of nodes that are allowed



Seismic risk assessment - overview

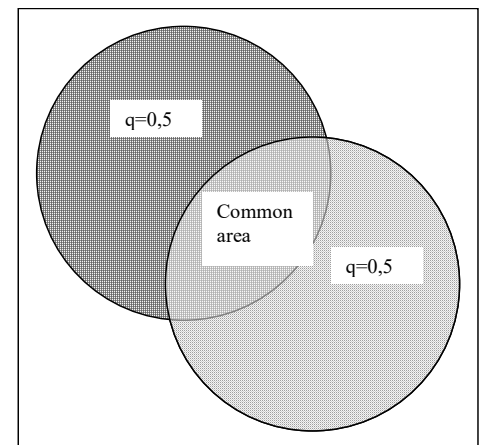
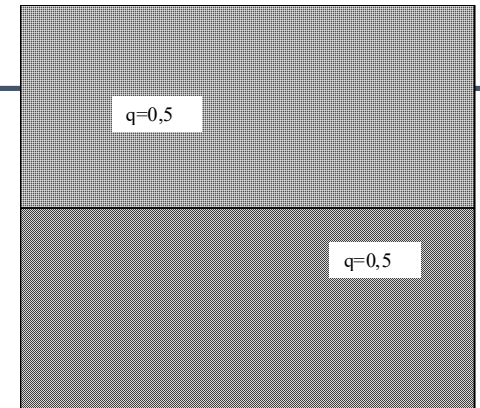
- For representation in a PSA model, the continuum of PGA values with associated frequencies is mostly divided into discrete intervals
 - Continuous range of PGA values is presented by successive seismic intervals
- For each interval the fragility for each component is decided
- Last intervals (high PGA) will cause very high probability of failure for components
- Normally, a standard MCUB solution may be too conservative

$$f_O^{(i)} = f_{E,L}^{(i)} - f_{E,U}^{(i)}$$



Mutual Exclusivity –What is that?

- When for example two events are dependent in following way:
 - $P_b = 1 - P_a$
- When might this be relevant?
 - Time fractions, for example system configuration probabilities
 - Maintenance unavailabilities that cannot occur at the same time
 - (CCF)



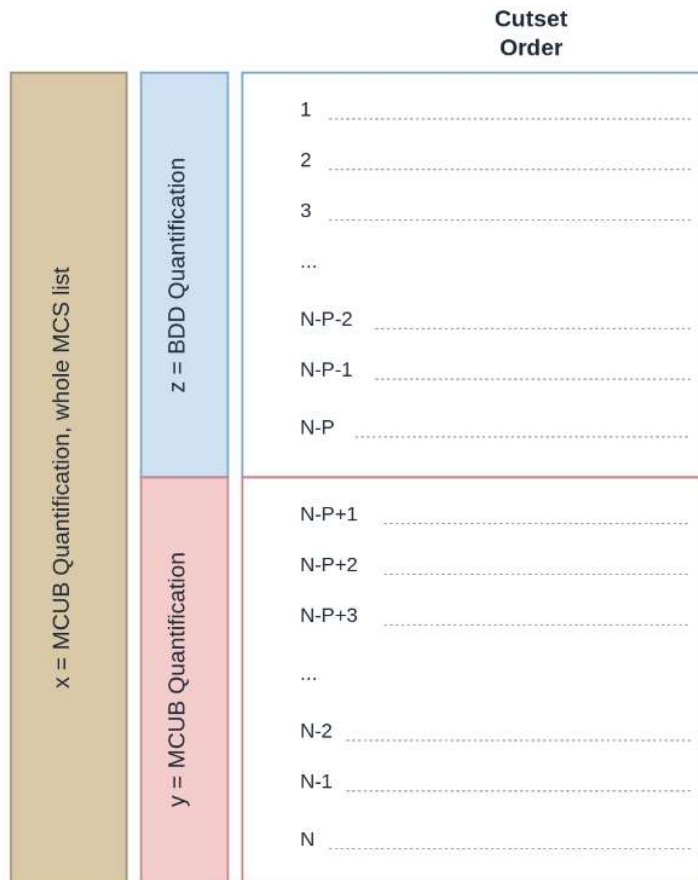
The purpose of this presentation

- The MCS BDD approach is very good – and scalable
 - Much better accuracy than normal MCUB calculation
- One potential issue has been identified:
 - High number of high probability events in combination with very many MCSs
 - Mutual exclusivity between events (not only frequency events)
- A situation where this can be relevant is seismic risk assessment, in the intervals with high PGAs

Basics



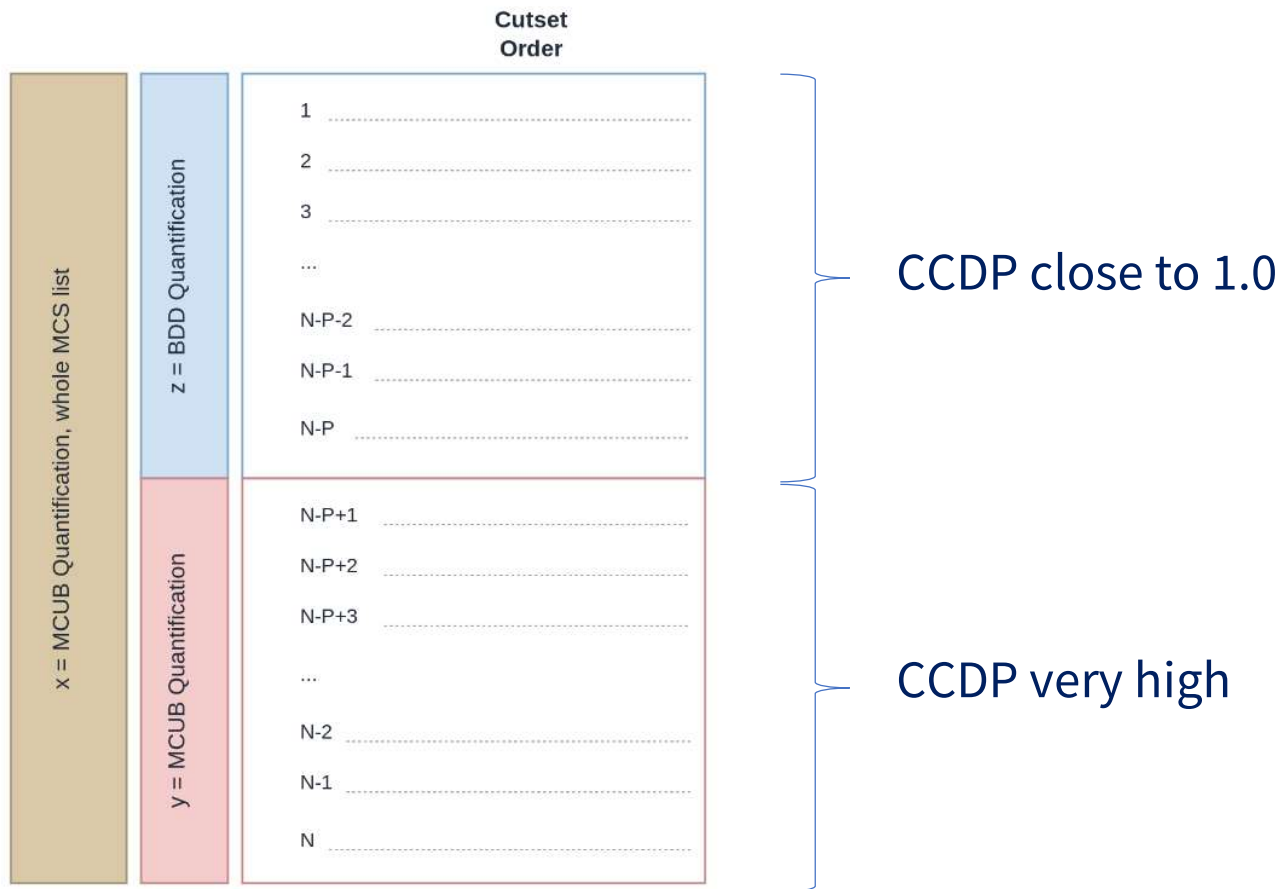
MCS BDD – Approximations



Seismic analyses

- MCS BDD
 - MUX
 - High values
 - MCS Limit used

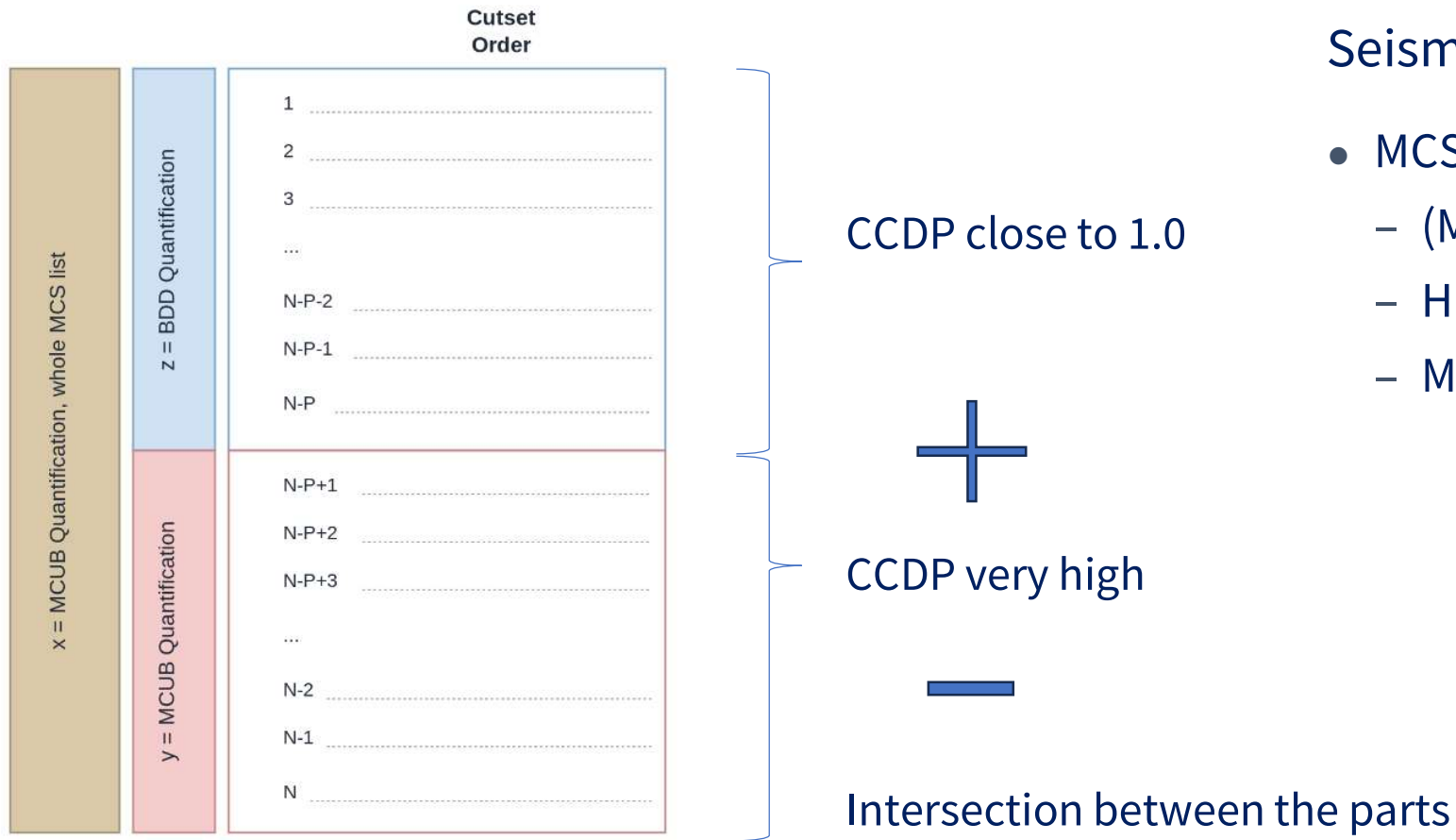
MCS BDD – Difficult Cases



Seismic analyses

- MCS BDD
 - MUX
 - High values
 - MCS Limit used

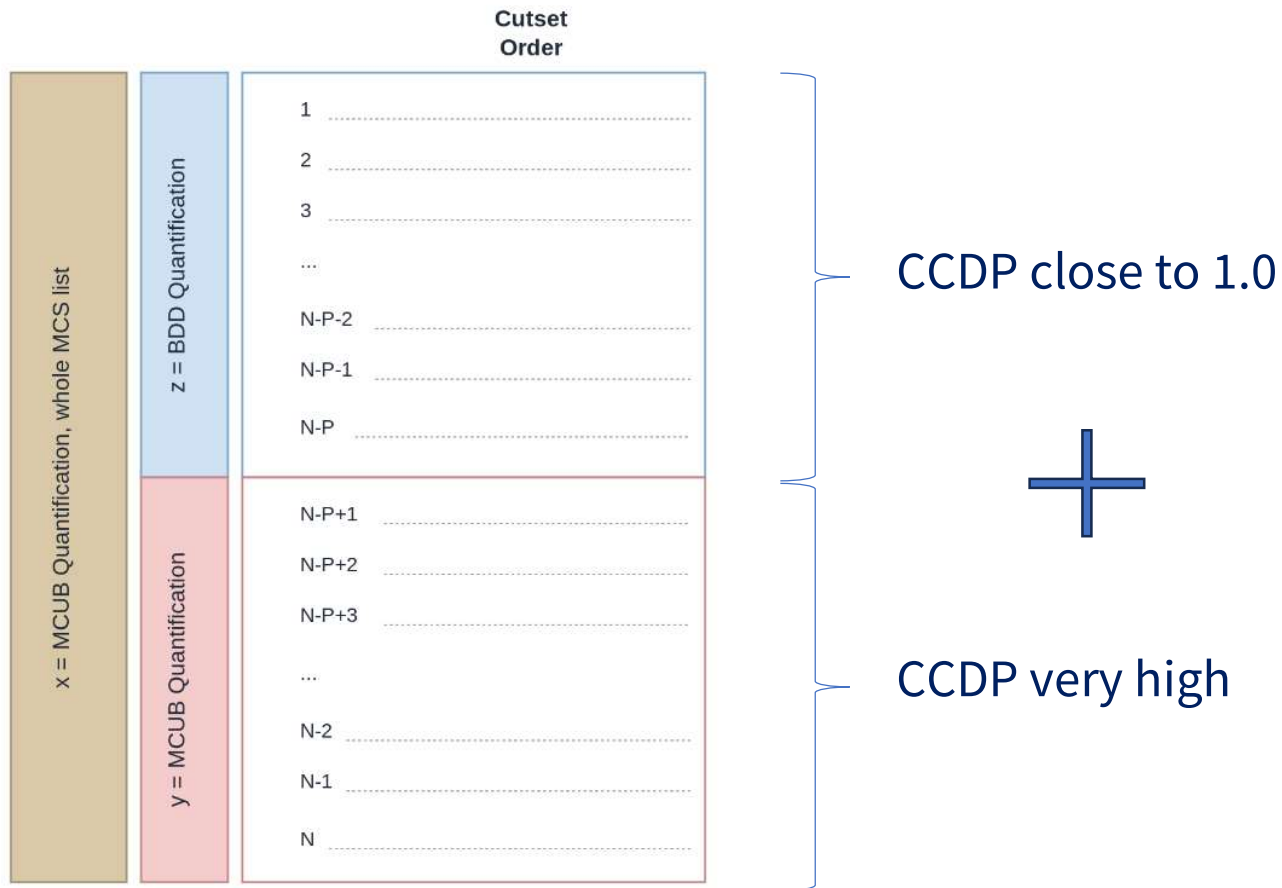
MCS BDD – Difficult Cases, but can be managed – no MUX



Seismic analyses

- MCS BDD
 - (MUX)
 - High values
 - MCS Limit used

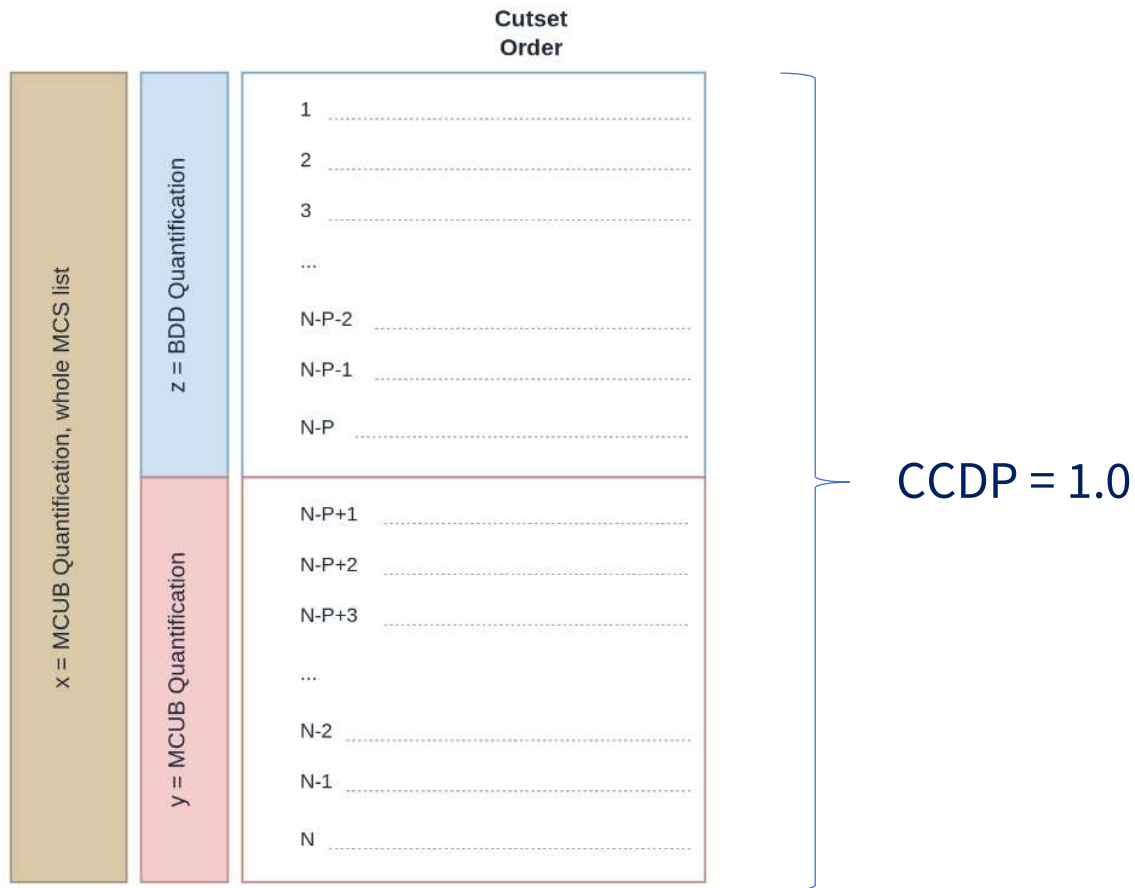
MCS BDD – Difficult Cases - MUX



Seismic analyses

- MCS BDD
 - MUX
 - High values
 - MCS Limit used

MCS BDD – Difficult Cases



Seismic analyses

- MCS BDD
 - MUX
 - High values
 - MCS Limit used

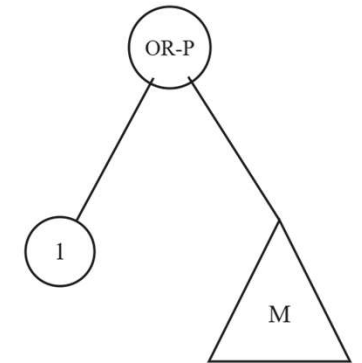
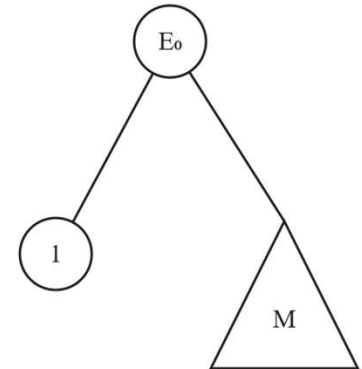
The improved approach



Basis for the improved algorithm

Case where there is no MUX present

- First, we notice that if the MCS below the MCS limit is only MCS represented by the probability of one event E_0 – it should be added to the BDD as a new node (M is denoting the representation of the BDD)
 - This will lead to the same approximation as if BDD and MCUB parts are added and then the intersection subtracted.
- Then we observe, what if we create an OR-module of all MCSs below the MCS limit (P is denoting the part below the MCS limit) – this can be added as a node to the BDD in a similar way
 - This will again lead to the same approximation as if BDD and MCUB parts are added and then the intersection subtracted.
- In fact – the event or module can be treated like any other event and be inserted into the BDD structure (Note that M is actually a BDD structure)



Basis for the improved algorithm

Including MUX

- Now, we observe that if we create different OR-modules – such that these are combined considering the other existing MUX events in the MCS (OR_A , OR_B etc)
 - Then such events can be inserted into the BDD structure in relevant places considering the other MUX events
- By this, the addition of the BDD and MCUB parts of the MCS list can consider the intersection of the overlapping parts – also when MUX is present

Conclusion



Conclusion

- We have introduced a potential accuracy issue in corner case scenarios – mostly relating to seismic risk in last intervals
- The solution is to modularize the part treated by MCUB into different OR modules and integrate them directly into the BDD structure
- MCS BDD approach is superior to MCUB cases, also in the corner case scenario

			Cutset Order
MCUB/Sum, Whole MCS list	Add MCUB P' as BDD-OR modules	M = BDD quant	1
			2
			3
			...
			B-2
			B-1
			B
		P' = BDD OR Modules	B+1
			B+2
			B+3
			...
			n-2
			n-1
			n
		P = MCUB quant	n+1
			n+2
			n+3
			...
			N-2
			N-1
			N

Thank you

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