

University of Stuttgart

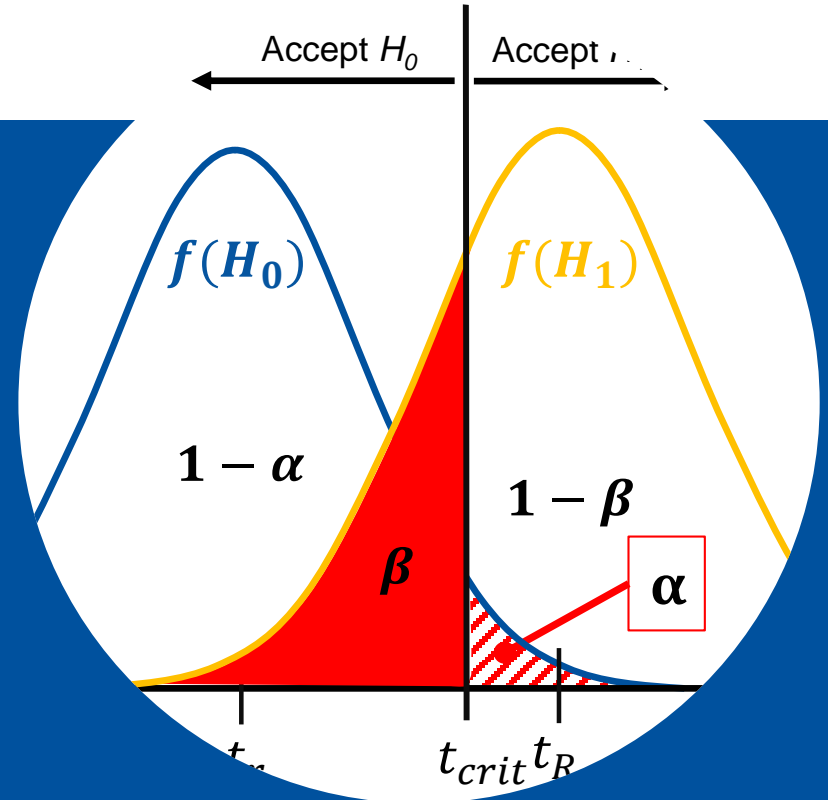
Institut für Maschinenelemente

Forschungsbereich Zuverlässigkeitstechnik

# Risk-based Reliability Demonstration Test Planning for Decision Making under Uncertainty

Probabilistic Safety Assessment and Management  
Conference (PSAM 16)

Dr.-Ing. Martin Dazer



# Scope

1

**Reliability research at the University of Stuttgart**

2

Decision making under Uncertainty

3

Risk based test planning procedure

4

Case studies

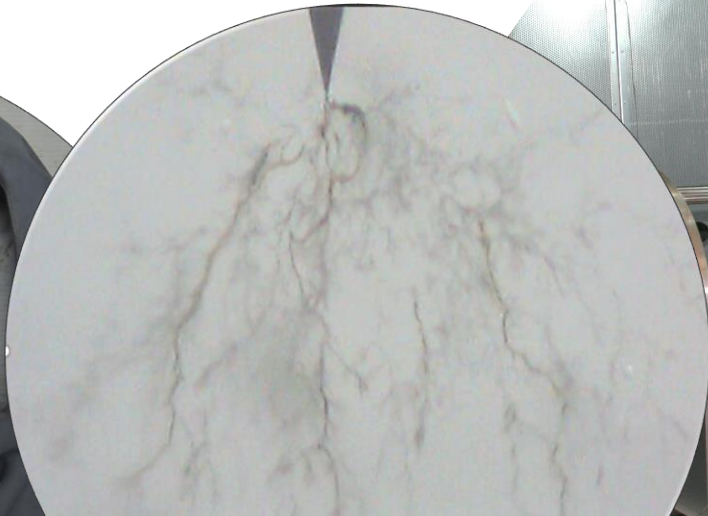
5

Summary

# Institute of Machine Components

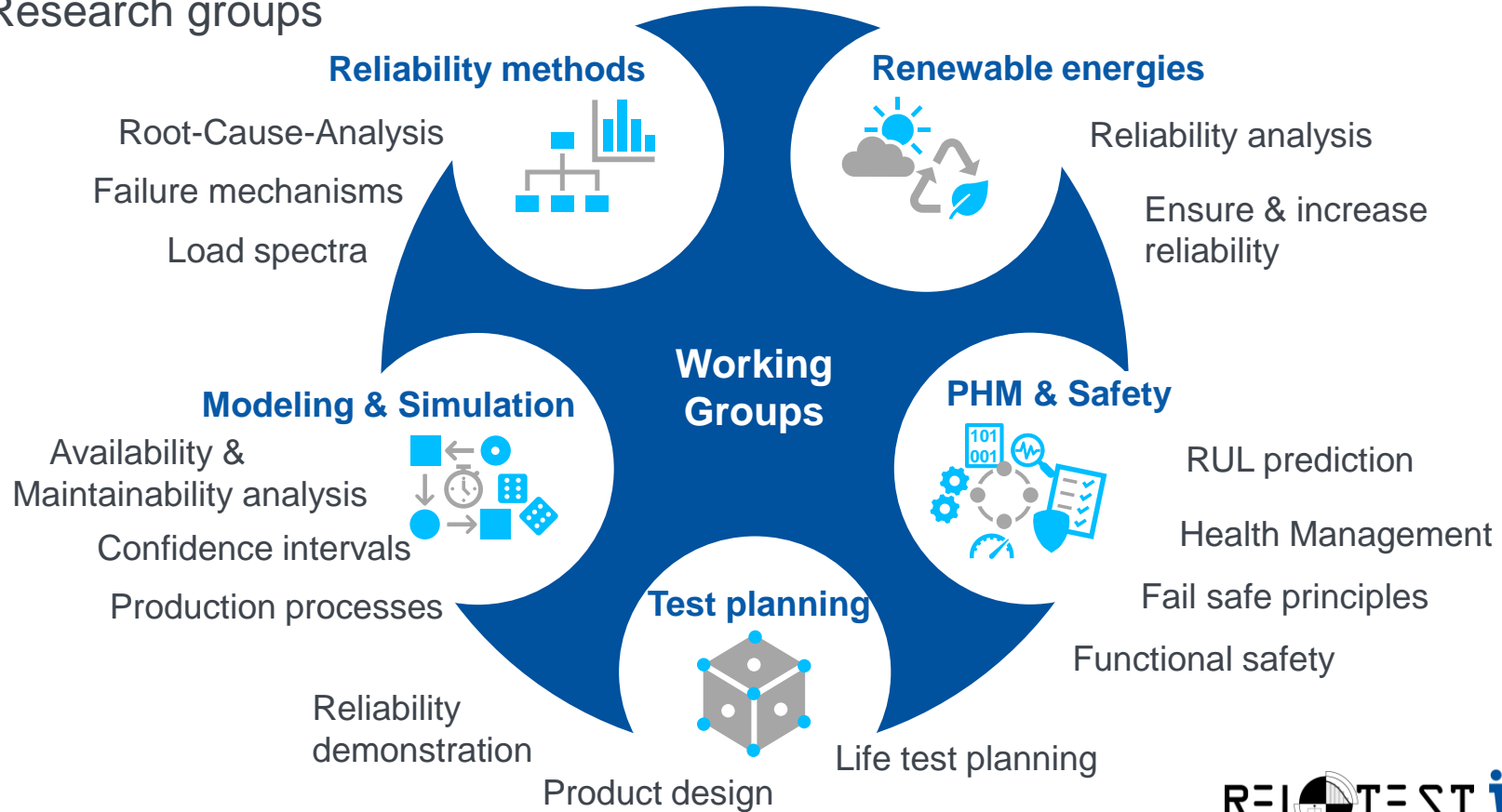
## Overview

- Research fields: Reliability Engineering, Sealing Technology, Driveline Technology, Rail Vehicle Technology
- Scientific staff: 2 profs, 5 doctors, about 35 PhD students
- App. 100 bachelor and master theses
- App. 50 publications yearly



# Institute of Machine Components

## Research groups



# Scope

1 Reliability research at the University of Stuttgart

**2 Decision making under uncertainty**

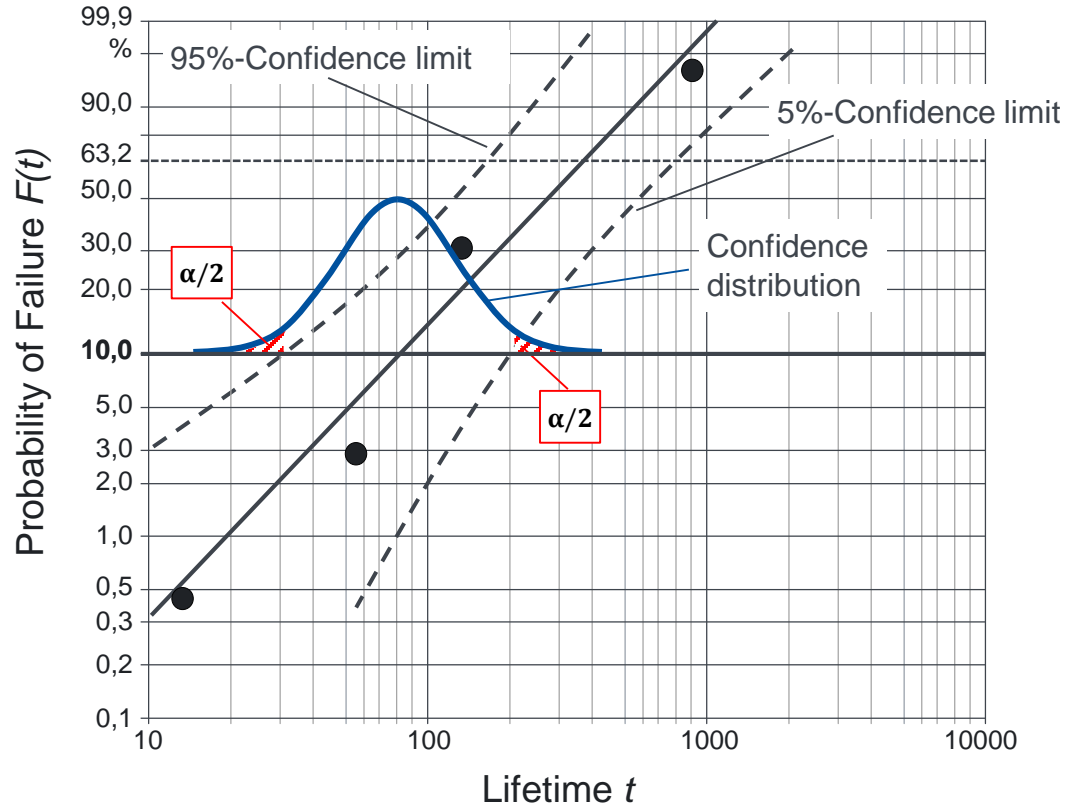
3 Risk based test planning procedure

4 Case studies

5 Summary

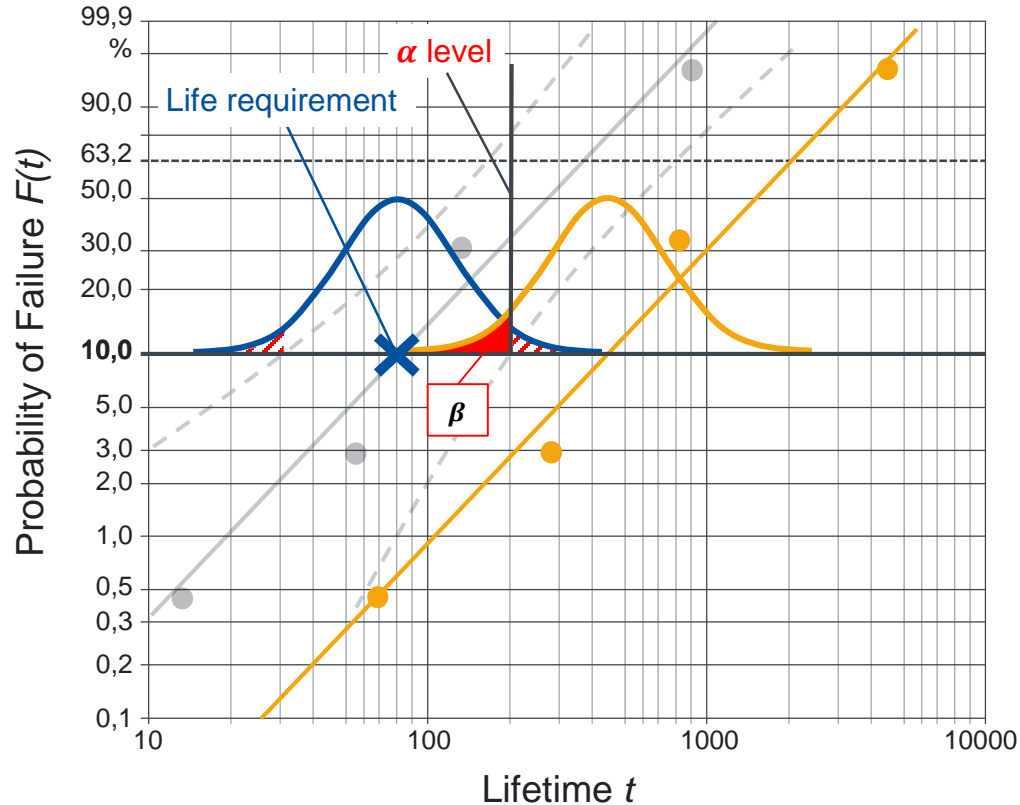
# Decision Making under Uncertainty

## Challenge



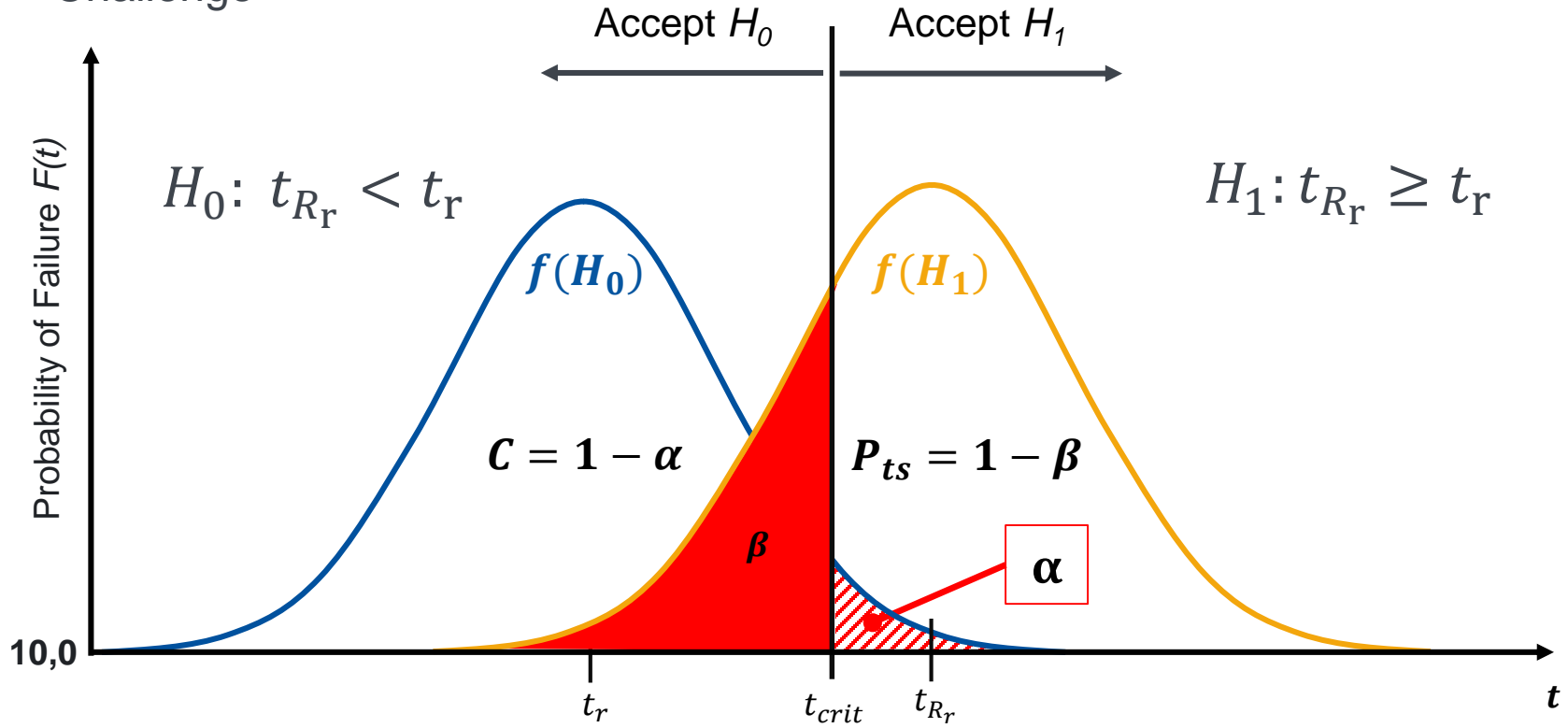
# Decision Making under Uncertainty

## Challenge



# Decision Making under Uncertainty

## Challenge





# Scope

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**Risk based test planning procedure**

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Summary

# Scope

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## Risk based test planning procedure

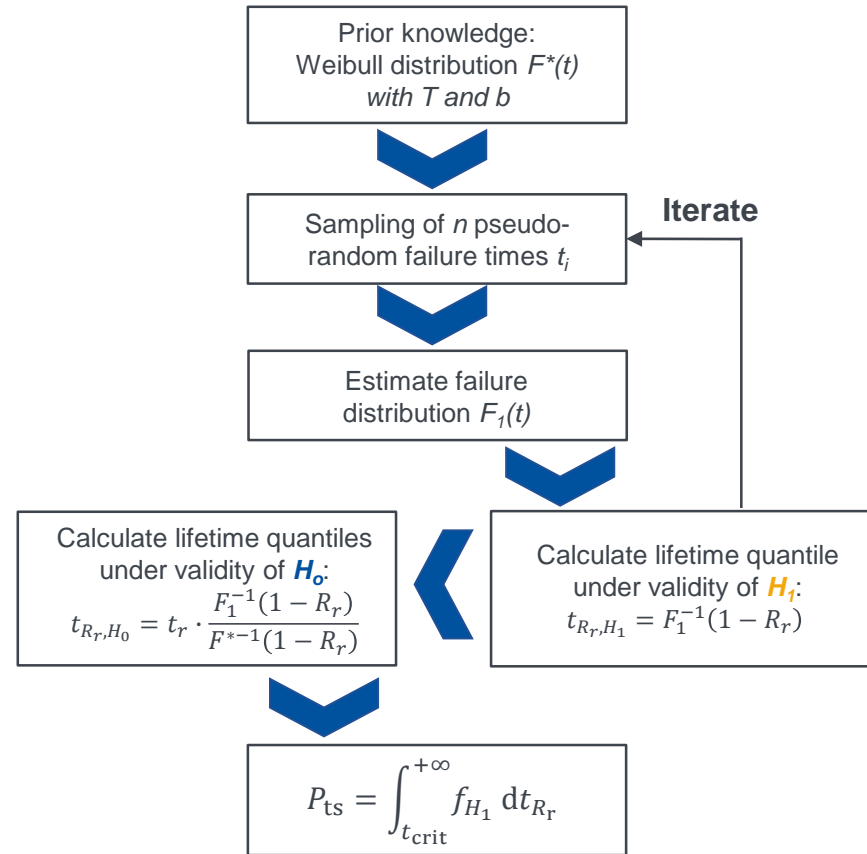
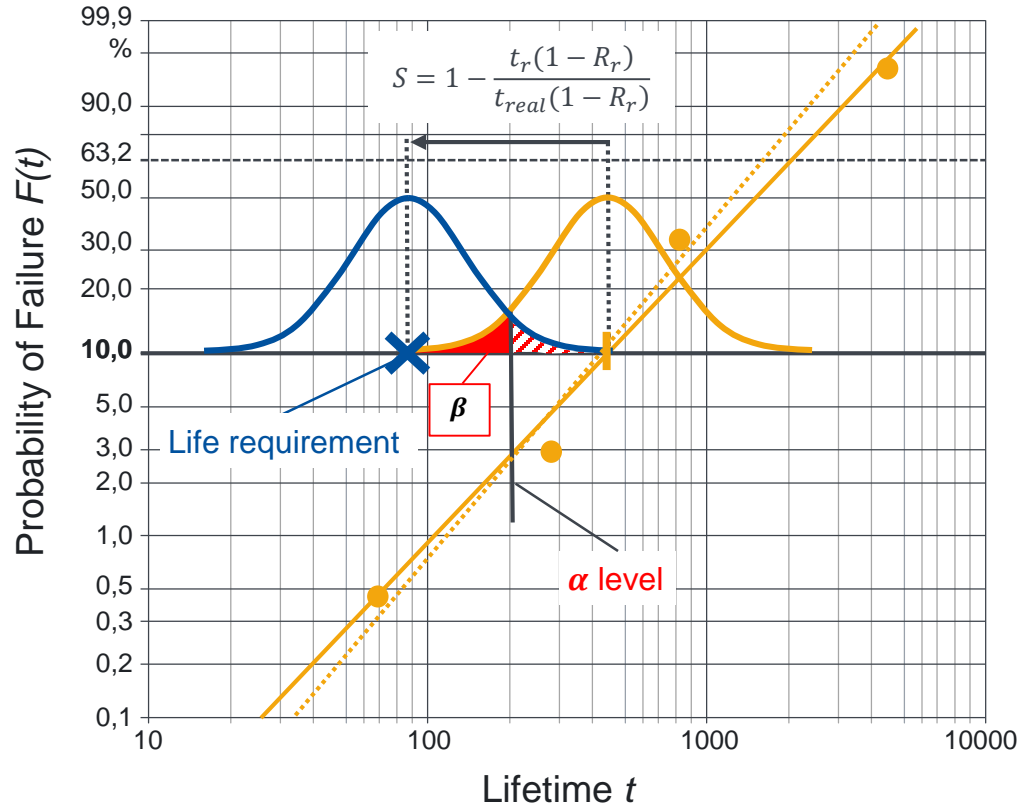
End-of-Life Test planning

Accelerated End-of-Life Test planning

Zero Failure Testing

# Risk based test planning procedure

## End-of-Life Testing



# Risk based test planning procedure

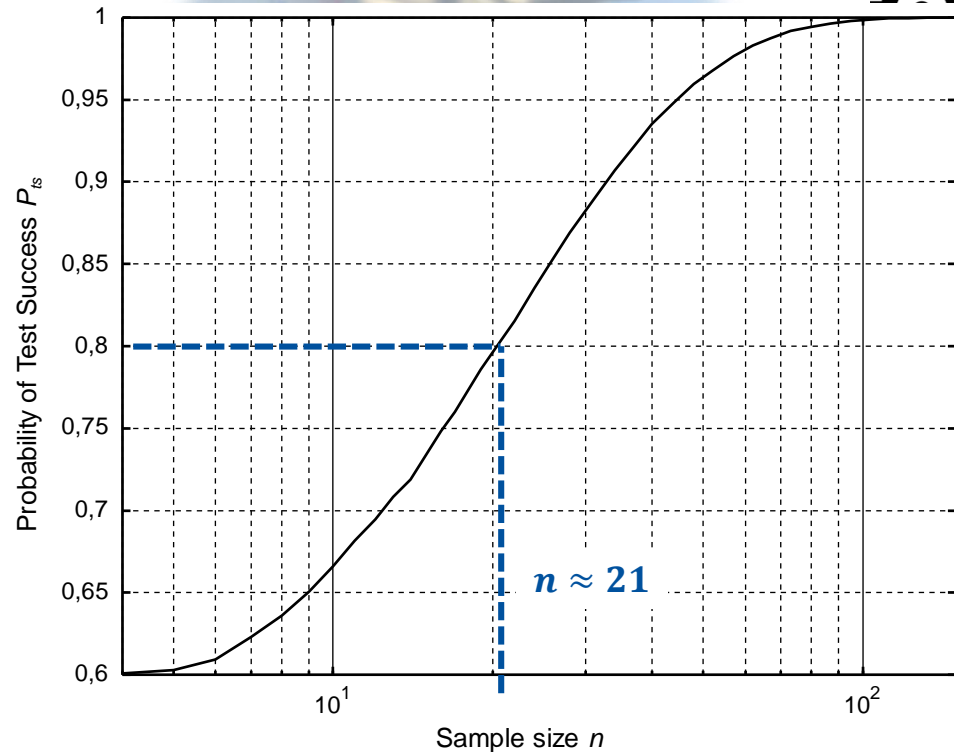
## End-of-Life Testing Case Study

### Requirements

Reliability	90 %
Confidence	90 %
Lifetime	$2 \cdot 10^6$ revolutions

### Prior knowledge

Shape $b$	3
Scale $T$	$6.06 \cdot 10^6$ revolutions



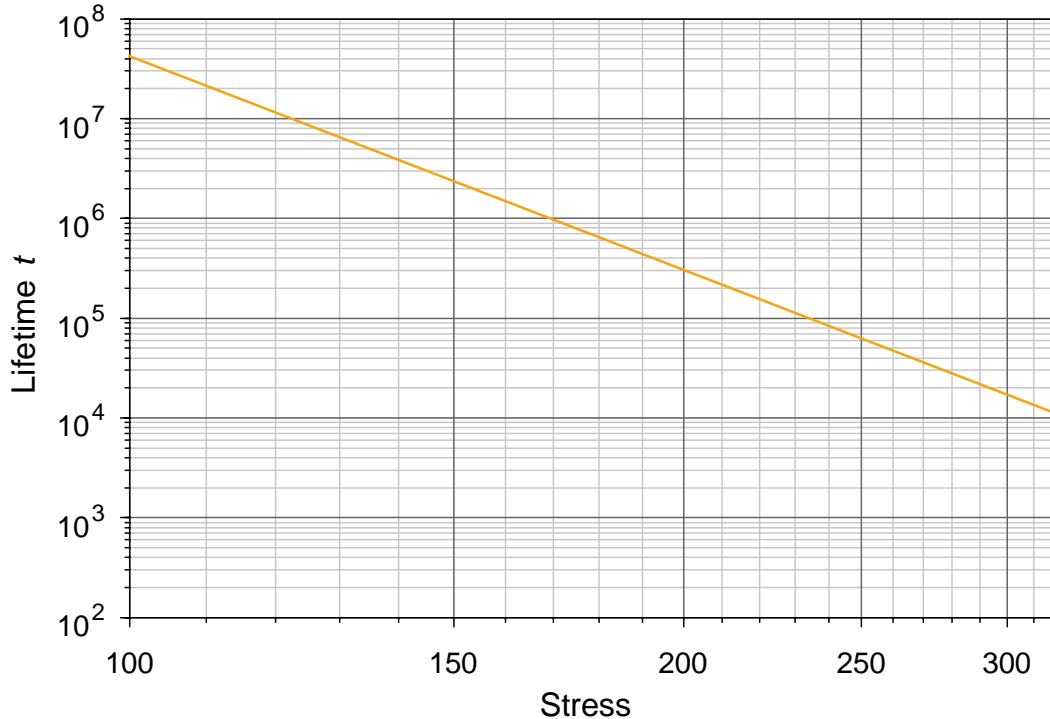
# Risk based test planning procedure

## Accelerated End-of-Life Testing

Life model:

$$\ln(T) = \ln(m_2) - \ln(B) \cdot m_1$$

$$\ln L = \sum_{i=1}^n \ln \left( \frac{b}{m_2 \cdot B^{-m_1}} \cdot \left( \frac{t_i}{m_2 \cdot B^{-m_1}} \right)^{b-1} \cdot e^{-\left( \frac{t_i}{m_2 \cdot B^{-m_1}} \right)^b} \right)$$



# Risk based test planning procedure

## Accelerated End-of-Life Testing

Life model:

$$\ln(T) = \ln(m_2) - \ln(B) \cdot m_1$$

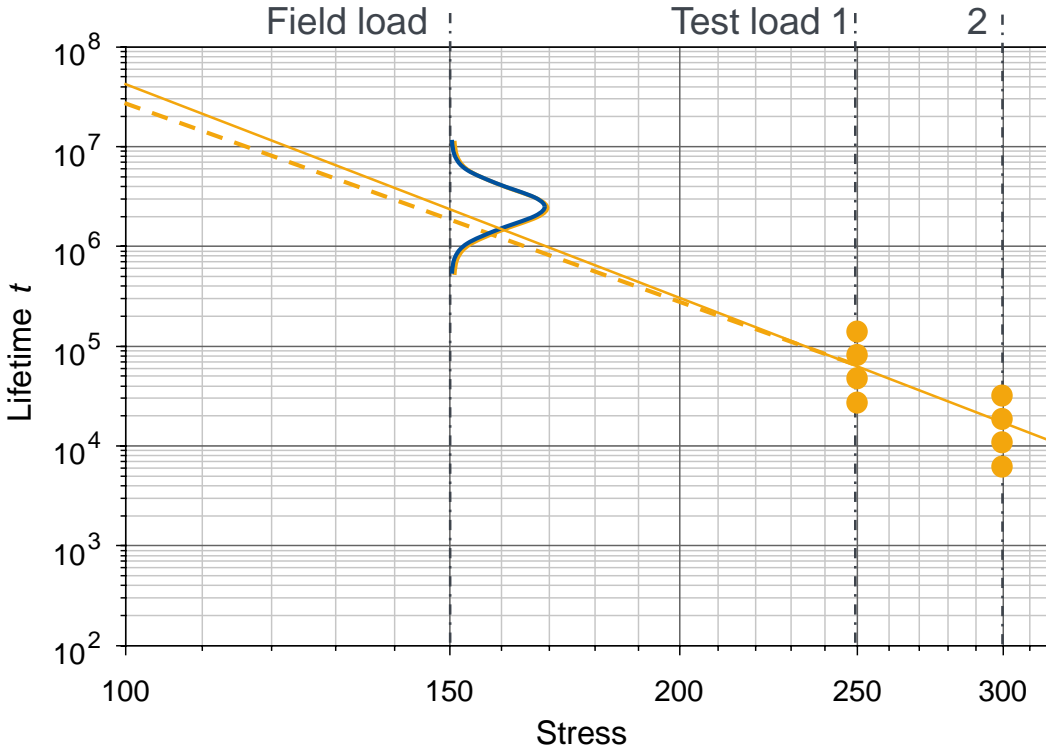
$$\ln L = \sum_{i=1}^n \ln \left( \frac{b}{m_2 \cdot B^{-m_1}} \cdot \left( \frac{t_i}{m_2 \cdot B^{-m_1}} \right)^{b-1} \cdot e^{-\left( \frac{t_i}{m_2 \cdot B^{-m_1}} \right)^b} \right)$$



Prior knowledge:  
Weibull distribution  $F^*(t)$   
with  $T$  and  $b$   
**Lifetime model parameters:**  
**Slope  $m_1$**   
**Baseline  $m_2$**

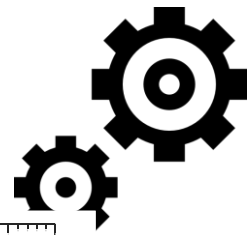


**Similar procedure to EoL**



# Risk based test planning procedure

## Accelerated End-of-Life Testing Case Study

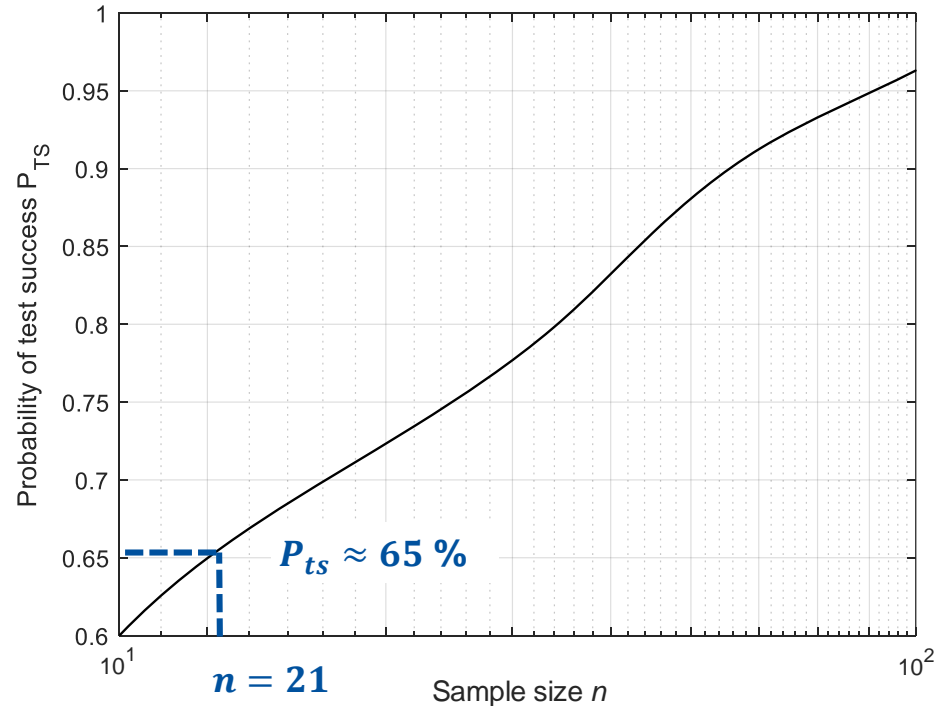


### Requirements

Reliability	90 %
Confidence	90 %
Lifetime	$2 \cdot 10^6$ revolutions

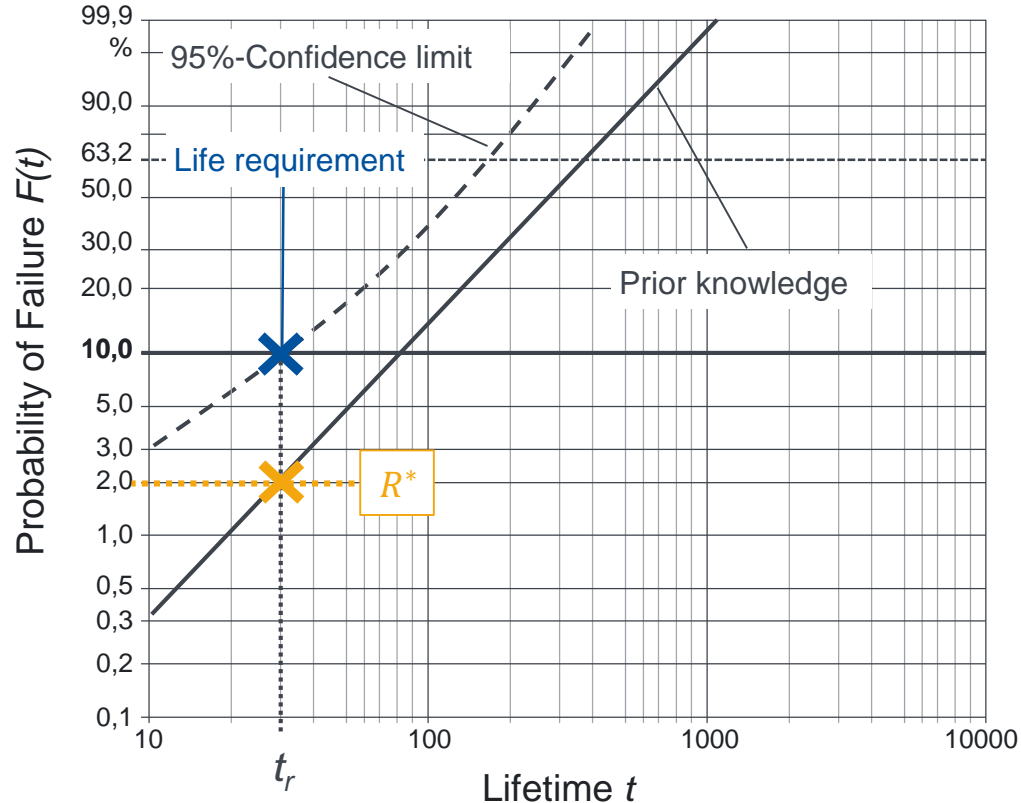
### Prior knowledge

Shape $b$	3
Scale $T$	$6.06 \cdot 10^6$ revolutions
Slope $k$	5



# Risk based test planning procedure

## Zero Failure Testing



$$H_0: R(t_r) < R_r(t_r)$$

$$H_1: R(t_r) \geq R_r(t_r)$$

$$C = 1 - \sum_{i=0}^f \binom{n_{SR}}{i} \cdot (R_r(t_r))^{n_{SR}-i} \cdot (1 - R_r(t_r))^i$$

$$P_{ts} = \sum_{i=0}^f \binom{n_{SR}}{i} \cdot (R^*(t_r))^{n_{SR}-i} \cdot (1 - R^*(t_r))^i$$

$$P_{ts} = (R^*(t_r))^{n_{SR}} \quad \text{with} \quad R^*(t_r) \approx e^{-\left(\frac{t_r}{T^*}\right)^{b^*}}$$



# Risk based test planning procedure

## Zero Failure Testing



$$C = 1 - \sum_{i=0}^f \binom{n_{SR}}{i} \cdot (R_r(t_r))^{n_{SR}-i} \cdot (1 - R_r(t_r))^i$$

$$n_{SR} = \frac{\ln(1 - C)}{\ln(R_r(t_r))} = 22$$

$$R^*(t_r) \approx e^{-\left(\frac{t_r}{T^*}\right)^b} = e^{-\left(\frac{30,000}{96,000}\right)^3} \approx 97 \%$$

$$P_{ts} = (R^*(t_r))^{n_{SR}} = (0,97)^{22} \approx 51 \%$$

### Requirements

Reliability	90 %
Confidence	90 %
Lifetime	30,000 cycles

### Prior knowledge

Shape $b$	3
Scale $T$	96,000 cycles

# Scope

1 Reliability research at the University of Stuttgart

2 Decision making under Uncertainty

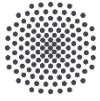
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5 **Summary**

# Summary

- Reliability test planning and reliability demonstration always take place under uncertainty.
- Decisions have to be made with minimum risk
- The  $P_{ts}$  quantifies the entrepreneurial risk of a failed reliability test
- All known reliability test strategies can be evaluated
- Possibility to identify the best possible test strategy for the individual use case just before decision making



**University of Stuttgart**

Institute of Machine Components

Reliability Department

**Thank you!**



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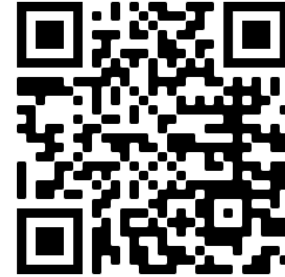
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